

CddInterface

Gap interface to Cdd package

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Chapter 1

Introduction

1.1 Why CddInterface

We know that every convex polyhedron has two representations, one as the intersection of finite half-spaces and the other as Minkowski sum of the convex hull of finite points and the nonnegative hull of finite directions. These are called H -representation and V -representation, respectively. CddInterface is a gap interface to the C package cddlib which among other things can translate between these two representations.

1.2 H -representation and V -representation of polyhedra

Let us start by introducing the H -representation. Let A be $m \times d$ matrix and let b be a column m -vector. The H -representation of the polyhedron defined by the system $b + Ax \geq 0$ of m inequalities and d variables $x = (x_1, \dots, x_d)$ is as follows:

```
Code
H-representation
linearity t, [i_1, i_2, ..., i_t]
begin
  m x (d+1) numbertype
  b A
end
```

The linearity line is added when we want to specify that some rows of the system $b + Ax$ are equalities. That is, $k \in \{i_1, i_2, \dots, i_t\}$ means that the row k of the system $b + Ax$ is specified to be equality.

For example, the H -representation of the polyhedron defined by the following system:

$$4 - 3x_1 + 6x_2 - 5x_4 = 0, 1 + 2x_1 - 2x_2 - 7x_3 \geq 0, -3x_2 + 5x_4 = 0;$$

is the following:

```
Code
H-representation
linearity 2, [1, 3]
begin
  3 x 5 rational
  4 -3 6 0 -5
  1 2 -2 -7 0
```

```

0 0 -3 0 5
end

```

Next we define Polyhedra *V*-format. Let P be represented by n generating points and s generating directions (rays) as

$$P = \text{conv}(v_1, \dots, v_n) + \text{nonneg}(r_{n+1}, \dots, r_{n+s}).$$

Then the Polyhedra *V*-format is for P is:

```

Code
V-representation
linearity t, [i_1, i_2, ..., i_t]
begin
(n+s) x (d+1) numbertype
1 v_1
: :
1 v_n
0 r_{n+1}
: :
0 r_{n+s}
end

```

In the above format the generating points and generating rays may appear mixed in arbitrary order. Linearity for *V*-representation specifies a subset of generators whose coefficients are relaxed to be free. That is, $k \in \{i_1, i_2, \dots, i_t\}$ specifies that the k -th generator is specified to be free. This means for each such a ray r_k , the line generated by r_k is in the polyhedron, and for each such a vertex v_k , its coefficient is no longer nonnegative but still the coefficients for all v_i 's must sum up to one.

For example the *V*-representation of the polyhedron defined as

$$P := \text{conv}((2, 3), (-2, -3), (-1, 2)) + \text{nonneg}((1, 2), (-1, -2), (1, 1))$$

```

Code
V-representation
linearity 2, [ 1, 3 ]
begin
4 x 3 rational
1 2 3
1 -1 2
0 1 2
0 1 1
end

```

Chapter 2

Creating polyhedra and their Operations

2.1 Creating a polyhedron

2.1.1 Cdd_PolyhedronByInequalities

▷ `Cdd_PolyhedronByInequalities(ineq[, linearities_list])` (function)

Returns: a CddPolyhedron

The function takes a list in which every entry represents an inequality (or equality). In case we want some entries to represent equalities we should refer in a second list to their indices.

Example

```
gap> A:= Cdd_PolyhedronByInequalities( [ [ 0, 1, 0 ], [ 0, 1, -1 ] ] );
<Polyhedron given by its H-representation>
gap> Display( A );
H-representation
begin
  2 X 3  rational

    0   1   0
    0   1  -1
end
gap> B:= Cdd_PolyhedronByInequalities( [ [ 0, 1, 0 ], [ 0, 1, -1 ] ], [ 2 ] );
<Polyhedron given by its H-representation>
gap> Display( B );
H-representation
linearity 1, [ 2 ]
begin
  2 X 3  rational

    0   1   0
    0   1  -1
end
```

2.1.2 Cdd_PolyhedronByGenerators

▷ `Cdd_PolyhedronByGenerators(genes[, linearities_list])` (function)

Returns: a CddPolyhedron

The function takes a list in which every entry represents a vertex in the ambient vector space. In case we want some vertices to be free (the vertex and its negative belong to the polyhedron) we should refer in a second list to their indices .

Example

```
gap> A:= Cdd_PolyhedronByGenerators( [ [ 0, 1, 3 ], [ 1, 4, 5 ] ] );
<Polyhedron given by its V-representation>
gap> Display( A );
V-representation
begin
  2 X 3  rational

    0  1  3
    1  4  5
end
gap> B:= Cdd_PolyhedronByGenerators( [ [ 0, 1, 3 ] ], [ 1 ] );
<Polyhedron given by its V-representation>
gap> Display( B );
V-representation
linearity 1, [ 1 ]
begin
  1 X 3  rational

    0  1  3
end
```

2.2 Some operations on a polyhedron

2.2.1 Cdd_FourierProjection (for IsCddPolyhedron, IsInt)

▷ Cdd_FourierProjection(P, i) (operation)

Returns: a CddPolyhedron

The function returns the Fourier projection of the polyhedron in the subspace $(O, x_1, \dots, x_{i-1}, x_{i+1}, \dots, x_n)$ after applying the Fourier elimination algorithm to get rid of the variable x_i .

To illustrate this projection, Let $P = \text{conv}((1, 2), (4, 5))$ in \mathbb{Q}^2 .

To find its projection on the subspace (O, x_1) , we apply the Fourier elimination to get rid of x_2

Example

```
gap> P := Cdd_PolyhedronByGenerators( [ [ 1, 1, 2 ], [ 1, 4, 5 ] ] );
<Polyhedron given by its V-representation>
gap> H := Cdd_H_Rep( P );
<Polyhedron given by its H-representation>
gap> Display( H );
H-representation
linearity 1, [ 3 ]
begin
  3 X 3  rational

    4  -1  0
   -1   1  0
   -1  -1  1
```

```

end
gap> P_x1 := Cdd_FourierProjection( H, 2);
<Polyhedron given by its H-representation>
gap> Display( P_x1 );
H-representation
linearity 1, [ 3 ]
begin
  3 X 3  rational

    4  -1  0
   -1   1  0
    0   0  1
end
gap> Display( Cdd_V_Rep( P_x1 ) );
V-representation
begin
  2 X 3  rational

    1  1  0
    1  4  0
end

```

Let again $Q = \text{Conv}((2,3,4), (2,4,5)) + \text{nonneg}((1,1,1))$, and let us compute its projection on (O, x_2, x_3)

Example

```

gap> Q := Cdd_PolyhedronByGenerators( [ [ 1, 2, 3, 4 ], [ 1, 2, 4, 5 ], [ 0, 1, 1, 1 ] ] );
<Polyhedron given by its V-representation>
gap> R := Cdd_H_Rep( Q );
<Polyhedron given by its H-representation>
gap> Display( R );
H-representation
linearity 1, [ 4 ]
begin
  4 X 4  rational

    2   1  -1   0
   -2   1   0   0
   -1  -1   1   0
   -1   0  -1   1
end
gap> P_x2_x3 := Cdd_FourierProjection( R, 1);
<Polyhedron given by its H-representation>
gap> Display( P_x2_x3 );
H-representation
linearity 2, [ 1, 3 ]
begin
  3 X 4  rational

   -1   0  -1   1
   -3   0   1   0
    0   1   0   0
end

```

```

gap> Display( Cdd_V_Rep( last ) );
V-representation
begin
  2 X 4  rational

  0  0  1  1
  1  0  3  4
end

```

2.3 Some operations on two polyhedrons

2.3.1 Cdd_IsContained (for IsCddPolyhedron, IsCddPolyhedron)

▷ Cdd_IsContained(P_1 , P_2) (operation)

Returns: true or false

The function returns true if P_1 is contained in P_2 , otherwise returns false.

Example

```

gap> A := Cdd_PolyhedronByInequalities( [ [ 10, -1, 1, 0 ],
> [ -24, 9, 2, 0 ], [ 1, 1, -1, 0 ], [ -23, -12, 1, 11 ] ], [ 4 ] );
<Polyhedron given by its H-representation>
gap> B := Cdd_PolyhedronByInequalities( [ [ 1, 0, 0, 0 ],
> [ -4, 1, 0, 0 ], [ 10, -1, 1, 0 ], [ -3, -1, 0, 1 ] ], [ 3, 4 ] );
<Polyhedron given by its H-representation>
gap> Cdd_IsContained( B, A );
true
gap> Display( Cdd_V_Rep( A ) );
V-representation
begin
  3 X 4  rational

  1  2  3  4
  1  4 -6  7
  0  1  1  1
end
gap> Display( Cdd_V_Rep( B ) );
V-representation
begin
  2 X 4  rational

  1  4 -6  7
  0  1  1  1
end

```

2.3.2 Cdd_Intersection (for IsCddPolyhedron, IsCddPolyhedron)

▷ Cdd_Intersection(P_1 , P_2) (operation)

Returns: a CddPolyhedron

The function returns the intersection of P_1 and P_2

Example

```

gap> A := Cdd_PolyhedronByInequalities( [ [ 3, 4, 5 ] ], [ 1 ] );;
gap> B := Cdd_PolyhedronByInequalities( [ [ 9, 7, 2 ] ], [ 1 ] );;
gap> C := Cdd_Intersection( A, B );;
gap> Display( Cdd_V_Rep( A ) );
V-representation
linearity 1, [ 2 ]
begin
  2 X 3  rational

    1  -3/4    0
    0   -5     4
end
gap> Display( Cdd_V_Rep( B ) );
V-representation
linearity 1, [ 2 ]
begin
  2 X 3  rational

    1  -9/7    0
    0   -2     7
end
gap> Display( Cdd_V_Rep( C ) );
V-representation
begin
  1 X 3  rational

    1  -13/9    5/9
end

```

2.3.3 \+ (for IsCddPolyhedron, IsCddPolyhedron)

▷ \+(P_1 , P_2)

(operation)

Returns: a CddPolyhedronThe function returns the Minkowski sum of P_1 and P_2 .

Example

```

gap> P := Cdd_PolyhedronByGenerators( [ [ 1, 2, 5 ], [ 0, 1, 2 ] ] );
< Polyhedron given by its V-representation >
gap> Q := Cdd_PolyhedronByGenerators( [ [ 1, 4, 6 ], [ 1, 3, 7 ], [ 0, 3, 1 ] ] );
< Polyhedron given by its V-representation >
gap> S := P+Q;
< Polyhedron given by its H-representation >
gap> V := Cdd_V_Rep( S );
< Polyhedron given by its V-representation >
gap> Display( V );
V-representation
begin
  4 X 3  rational

    0   3   1
    1   6  11
    1   5  12

```

```
      0   1   2
end
gap> Cdd_GeneratingVertices( P );
[ [ 2, 5 ] ]
gap> Cdd_GeneratingVertices( Q );
[ [ 3, 7 ], [ 4, 6 ] ]
gap> Cdd_GeneratingVertices( S );
[ [ 5, 12 ], [ 6, 11 ] ]
gap> Cdd_GeneratingRays( P );
[ [ 1, 2 ] ]
gap> Cdd_GeneratingRays( Q );
[ [ 3, 1 ] ]
gap> Cdd_GeneratingRays( S );
[ [ 1, 2 ], [ 3, 1 ] ]
```

Chapter 3

Linear Programs

3.1 Creating and solving linear programs

3.1.1 Cdd_LinearProgram (for IsCddPolyhedron, IsString, IsList)

▷ Cdd_LinearProgram(*P*, *str*, *obj*) (operation)

Returns: a *CddLinearProgram* Object

The function takes three variables. The first is a polyhedron *poly*, the second *str* should be "max" or "min" and the third *obj* is the objective function.

3.1.2 Cdd_SolveLinearProgram (for IsCddLinearProgram)

▷ Cdd_SolveLinearProgram(*lp*) (operation)

Returns: a list if the program is optimal, otherwise returns the value 0

The function takes a linear program. If the program is optimal, the function returns a list of two entries, the solution vector and the optimal value of the objective, otherwise it returns *fail*.

To illustrate the using of these functions, let us solve the linear program given by:

Maximize $P(x,y) = 1 - 2x + 5y$, with

$$100 \leq x \leq 200, 80 \leq y \leq 170, y \geq -x + 200.$$

We bring the inequalities to the form $b + AX \geq 0$ and get:

$$-100 + x \geq 0, 200 - x \geq 0, -80 + y \geq 0, 170 - y \geq 0, -200 + x + y \geq 0.$$

Example

```
gap> A:= Cdd_PolyhedronByInequalities( [ [ -100, 1, 0 ], [ 200, -1, 0 ],
> [ -80, 0, 1 ], [ 170, 0, -1 ], [ -200, 1, 1 ] ] );
<Polyhedron given by its H-representation>
gap> lp1:= Cdd_LinearProgram( A, "max", [1, -2, 5 ] );
<Linear program>
gap> Display( lp1 );
Linear program given by:
H-representation
begin
  5 X 3  rational
```

```

-100    1    0
 200   -1    0
 -80    0    1
 170    0   -1
-200    1    1
end
max [ 1, -2, 5 ]
gap> Cdd_SolveLinearProgram( lp1 );
[ [ 100, 170 ], 651 ]
gap> lp2:= Cdd_LinearProgram( A, "min", [ 1, -2, 5 ] );
<Linear program>
gap> Display( lp2 );
Linear program given by:
H-representation
begin
  5 X 3  rational

-100    1    0
 200   -1    0
 -80    0    1
 170    0   -1
-200    1    1
end
min [ 1, -2, 5 ]
gap> Cdd_SolveLinearProgram( lp2 );
[ [ 200, 80 ], 1 ]
gap> B:= Cdd_V_Rep( A );
<Polyhedron given by its V-representation>
gap> Display( B );
V-representation
begin
  5 X 3  rational

 1  100  170
 1  100  100
 1  120   80
 1  200   80
 1  200  170
end

```

So the optimal solution for lp1 is $(x = 100, y = 170)$ with optimal value $p = 1 - 2(100) + 5(170) = 651$ and for lp2 is $(x = 200, y = 80)$ with optimal value $p = 1 - 2(200) + 5(80) = 1$.

Chapter 4

Attributes and properties

4.1 Attributes and properties of polyhedron

4.1.1 Cdd_Canonicalize (for IsCddPolyhedron)

▷ Cdd_Canonicalize(P) (attribute)

Returns: a CddPolyhedron

The function takes a polyhedron and reduces its defining inequalities (generators set) by deleting all redundant inequalities (generators).

Example

```
gap> A:= Cdd_PolyhedronByInequalities( [ [ 0, 2, 6 ], [ 0, 1, 3 ], [1, 4, 10 ] ] );
<Polyhedron given by its H-representation>
gap> B:= Cdd_Canonicalize( A );
<Polyhedron given by its H-representation>
gap> Display( B );
H-representation
begin
  2 X 3  rational

    0   1   3
    1   4  10
end
```

4.1.2 Cdd_V_Rep (for IsCddPolyhedron)

▷ Cdd_V_Rep(P) (attribute)

Returns: a CddPolyhedron

The function takes a polyhedron and returns its reduced V -representation.

4.1.3 Cdd_H_Rep (for IsCddPolyhedron)

▷ Cdd_H_Rep(P) (attribute)

Returns: a CddPolyhedron

The function takes a polyhedron and returns its reduced H -representation.

Example

```
gap> A:= Cdd_PolyhedronByInequalities( [ [ 0, 1, 1 ], [ 0, 5, 5 ] ] );
<Polyhedron given by its H-representation>
```

```

gap> B:= Cdd_V_Rep( A );
<Polyhedron given by its V-representation>
gap> Display( B );
V-representation
linearity 1, [ 2 ]
begin
  2 X 3  rational

    0   1   0
    0  -1   1
end
gap> C:= Cdd_H_Rep( B );
<Polyhedron given by its H-representation>
gap> Display( C );
H-representation
begin
  1 X 3  rational

    0   1   1
end
gap> D:= Cdd_PolyhedronByInequalities( [ [ 0, 1, 1, 34, 22, 43 ],
> [ 11, 2, 2, 54, 53, 221 ], [33, 23, 45, 2, 40, 11 ] ] );
<Polyhedron given by its H-representation>
gap> Cdd_V_Rep( D );
<Polyhedron given by its V-representation>
gap> Display( last );
V-representation
linearity 2, [ 5, 6 ]
begin
  6 X 6  rational

    1  -743/14  369/14  11/14      0      0
    0   -1213    619     22      0      0
    0      -1      1      0      0      0
    0     764   -390    -11      0      0
    0  -13526   6772     99     154     0
    0 -116608  59496   1485      0    154
end

```

4.1.4 Cdd_AmbientSpaceDimension (for IsCddPolyhedron)

- ▷ Cdd_AmbientSpaceDimension(P) (attribute)
Returns: The dimension of the ambient space of the polyhedron(i.e., the space that contains P).

4.1.5 Cdd_Dimension (for IsCddPolyhedron)

- ▷ Cdd_Dimension(P) (attribute)
Returns: The dimension of the polyhedron, where the dimension, $\dim(P)$, of a polyhedron P is the maximum number of affinely independent points in P minus 1.

4.1.6 Cdd_GeneratingVertices (for IsCddPolyhedron)

- ▷ Cdd_GeneratingVertices(P) (attribute)
Returns: The reduced generating vertices of the polyhedron

4.1.7 Cdd_GeneratingRays (for IsCddPolyhedron)

- ▷ Cdd_GeneratingRays(P) (attribute)
Returns: list
 The output is the reduced generating rays of the polyhedron

4.1.8 Cdd_Equalities (for IsCddPolyhedron)

- ▷ Cdd_Equalities(P) (attribute)
Returns: a list
 The output is the reduced equalities of the polyhedron.

4.1.9 Cdd_Inequalities (for IsCddPolyhedron)

- ▷ Cdd_Inequalities(P) (attribute)
 The output is the reduced inequalities of the polyhedron.

4.1.10 Cdd_InteriorPoint (for IsCddPolyhedron)

- ▷ Cdd_InteriorPoint(P) (attribute)
Returns: a list
 The output is an interior point in the polyhedron

4.1.11 Cdd_Faces (for IsCddPolyhedron)

- ▷ Cdd_Faces(P) (attribute)
Returns: a list
 This function takes a H -represented polyhedron P and returns a list. Every entry in this list is a again a list, contains the dimension and linearity of the face defined as a polyhedron over the same system of inequalities.

4.1.12 Cdd_FacesWithFixedDimension (for IsCddPolyhedron, IsInt)

- ▷ Cdd_FacesWithFixedDimension(P, d) (operation)
Returns: a list
 This function takes a H -represented polyhedron P and a positive integer d . The output is a list. Every entry in this list is the linearity of an d - dimensional face of P defined as a polyhedron over the same system of inequalities.

4.1.13 Cdd_FacesWithInteriorPoints (for IsCddPolyhedron)

▷ Cdd_FacesWithInteriorPoints(P) (attribute)

Returns: a list

This function takes a H -represented polyhedron P and returns a list. Every entry in this list is a again a list, contains the dimension, linearity of the face defined as a polyhedron over the same system of inequalities and an interior point in the face.

4.1.14 Cdd_FacesWithFixedDimensionAndInteriorPoints (for IsCddPolyhedron, IsInt)

▷ Cdd_FacesWithFixedDimensionAndInteriorPoints(P, d) (operation)

Returns: a list

This function takes a H -represented polyhedron P and a positive integer d . The output is a list. Every entry in this list is a again a list, contains the linearity of the face defined as a polyhedron over the same system of inequalities and an interior point in this face.

4.1.15 Cdd_Facets (for IsCddPolyhedron)

▷ Cdd_Facets(P) (attribute)

Returns: a list

This function takes a H -represented polyhedron P and returns a list. Every entry in this is the linearity of a facet defined as a polyhedron over the same system of inequalities.

4.1.16 Cdd_Lines (for IsCddPolyhedron)

▷ Cdd_Lines(P) (attribute)

Returns: a list

This function takes a H -represented polyhedron P and returns a list. Every entry in this is the linearity of a ray (1-dimensional face) defined as a polyhedron over the same system of inequalities.

4.1.17 Cdd_Vertices (for IsCddPolyhedron)

▷ Cdd_Vertices(P) (attribute)

Returns: a list

This function takes a H -represented polyhedron P and returns a list. Every entry in this list is the linearity of a vertex defined as a polyhedron over the same system of inequalities.

4.1.18 Cdd_IsEmpty (for IsCddPolyhedron)

▷ Cdd_IsEmpty(P) (property)

Returns: true or false

The output is true if the polyhedron is empty and false otherwise

4.1.19 Cdd_IsCone (for IsCddPolyhedron)

▷ Cdd_IsCone(P) (property)

Returns: true or false

The output is true if the polyhedron is cone and false otherwise

4.1.20 Cdd_IsPointed (for IsCddPolyhedron)

▷ Cdd_IsPointed(P)

(property)

Returns: true or false

The output is true if the polyhedron is pointed and false otherwise

Example

```
gap> poly:= Cdd_PolyhedronByInequalities( [ [ 1, 3, 4, 5, 7 ], [ 1, 3, 5, 12, 34 ],
> [ 9, 3, 0, 2, 13 ] ], [ 1 ] );
<Polyhedron given by its H-representation>
gap> Cdd_InteriorPoint( poly );
[ -194/75, 46/25, -3/25, 0 ]
gap> Cdd_FacesWithInteriorPoints( poly );
[ [ 3, [ 1 ], [ -194/75, 46/25, -3/25, 0 ] ], [ 2, [ 1, 2 ],
[ -62/25, 49/25, -7/25, 0 ] ], [ 1, [ 1, 2, 3 ],
[ -209/75, 56/25, -8/25, 0 ] ], [ 2, [ 1, 3 ], [ -217/75, 53/25, -4/25, 0 ] ] ]
gap> Cdd_Dimension( poly );
3
gap> Cdd_IsPointed( poly );
false
gap> Cdd_IsEmpty( poly );
false
gap> Cdd_Faces( poly );
[ [ 3, [ 1 ] ], [ 2, [ 1, 2 ] ], [ 1, [ 1, 2, 3 ] ], [ 2, [ 1, 3 ] ] ]
gap> poly1 := Cdd_ExtendLinearity( poly, [ 1, 2, 3 ] );
<Polyhedron given by its H-representation>
gap> Display( poly1 );
H-representation
linearity 3, [ 1, 2, 3 ]
begin
  3 X 5   rational

    1   3   4   5   7
    1   3   5  12  34
    9   3   0   2  13
end
gap> Cdd_Dimension( poly1 );
1
gap> Cdd_Facets( poly );
[ [ 1, 2 ], [ 1, 3 ] ]
gap> Cdd_GeneratingVertices( poly );
[ [ -209/75, 56/25, -8/25, 0 ] ]
gap> Cdd_GeneratingRays( poly );
[ [ -97, 369, -342, 75 ], [ -8, -9, 12, 0 ],
[ 23, -21, 3, 0 ], [ 97, -369, 342, -75 ] ]
gap> Cdd_Inequalities( poly );
[ [ 1, 3, 5, 12, 34 ], [ 9, 3, 0, 2, 13 ] ]
gap> Cdd_Equalities( poly );
[ [ 1, 3, 4, 5, 7 ] ]
gap> P := Cdd_FourierProjection( poly, 2);
<Polyhedron given by its H-representation>
gap> Display( P );
H-representation
linearity 1, [ 3 ]
```

```
begin
  3 X 5  rational

    9    3    0    2   13
   -1   -3    0   23  101
    0    0    1    0    0
end
```

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